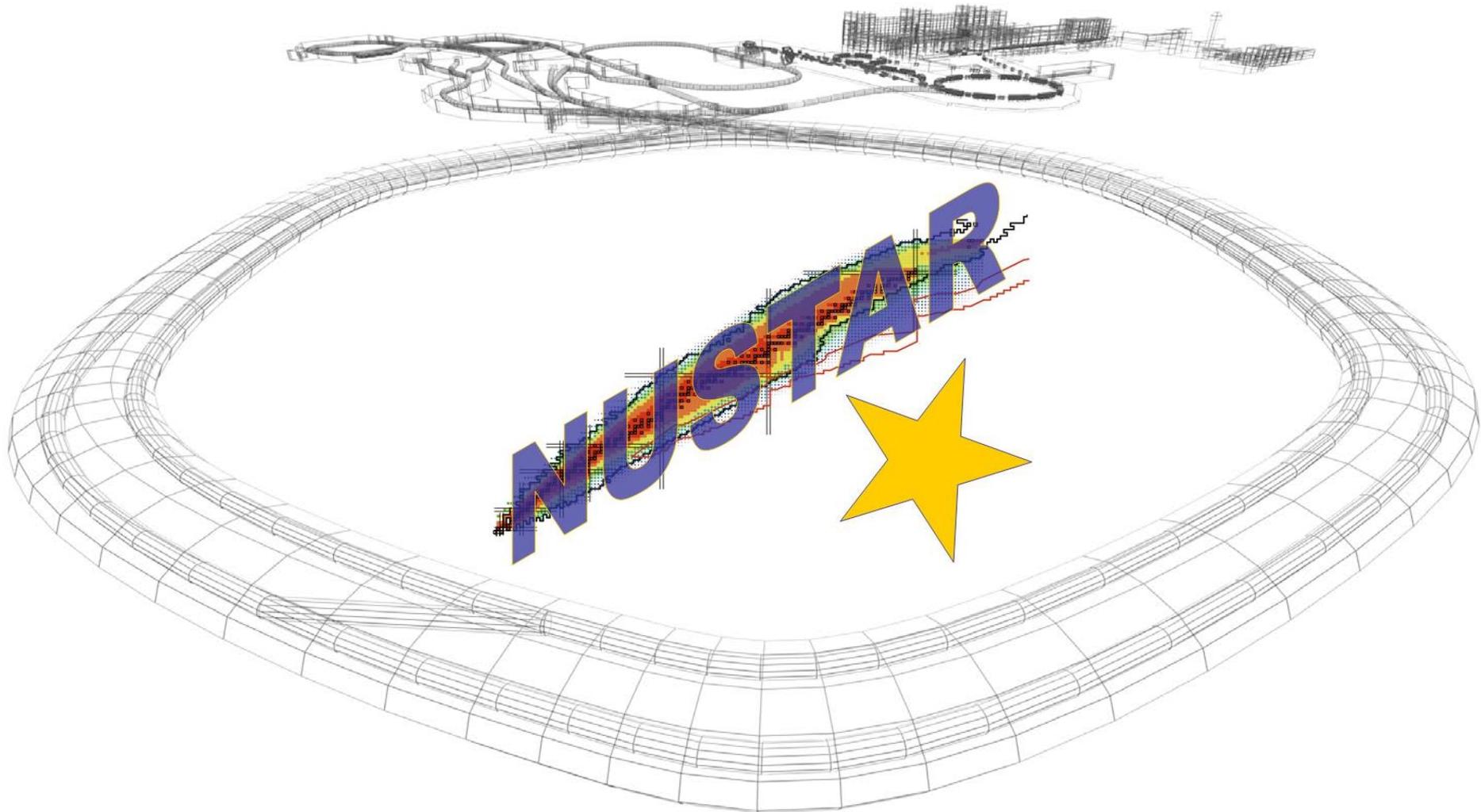


Physics with Exotic Nuclei

Hans-Jürgen Wollersheim



NUclear **ST**tructure, **A**strophysics and **R**eaction

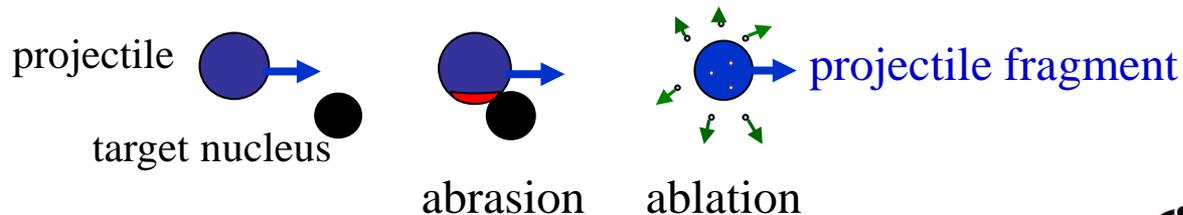
Outline

❖ Projectile Fragmentation – A Route to Exotic Nuclei

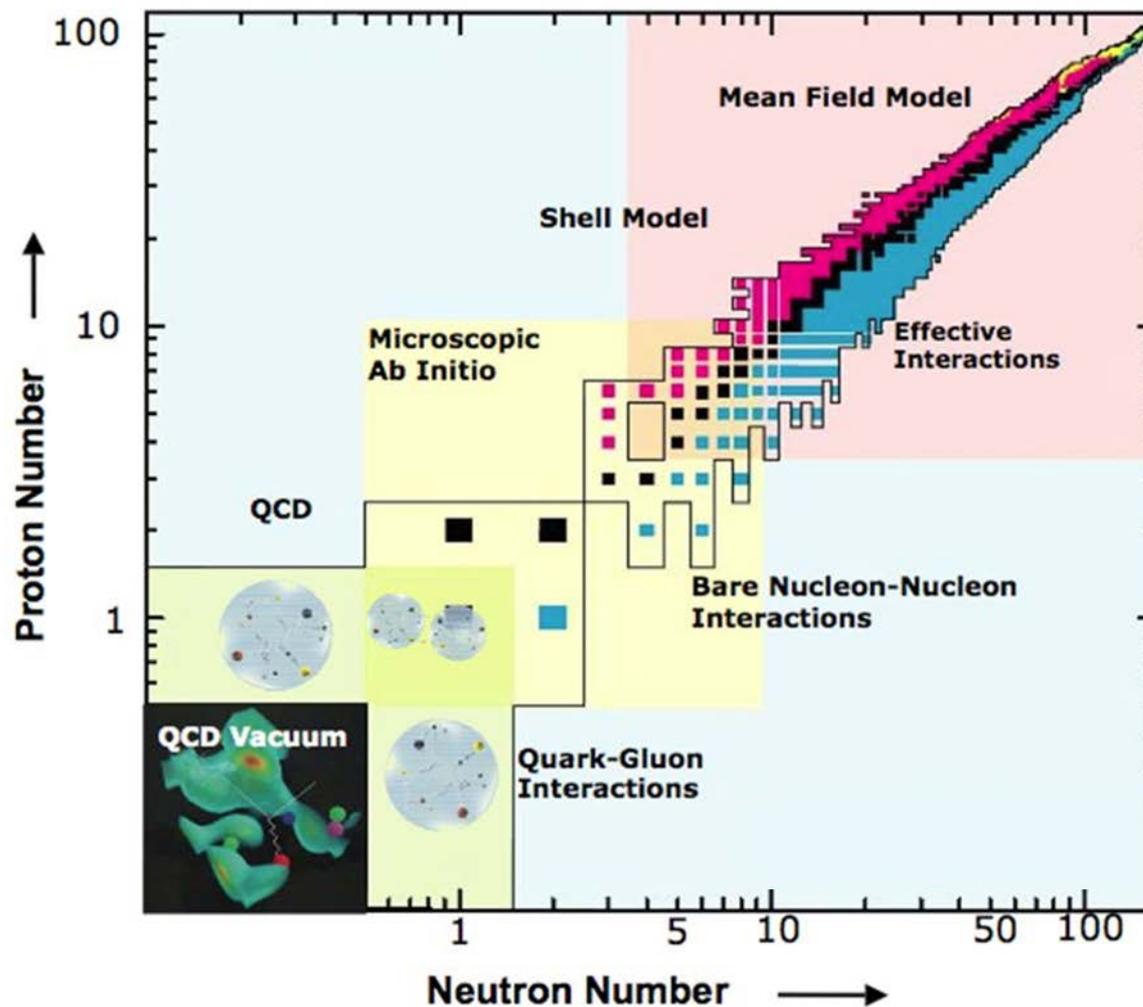
- Fragmentation Cross Sections
- Nuclear Reaction Rates
- In-Flight Separation of **R**adioactive **I**on **B**eams
- **F**Ragment **S**eparator at GSI
- Comparison FRS – Super-FRS
- Identification of **RIBs**

❖ Excited Fragments – Gateway to Nuclear Structure

❖ Scattering Experiments with **RIBs**

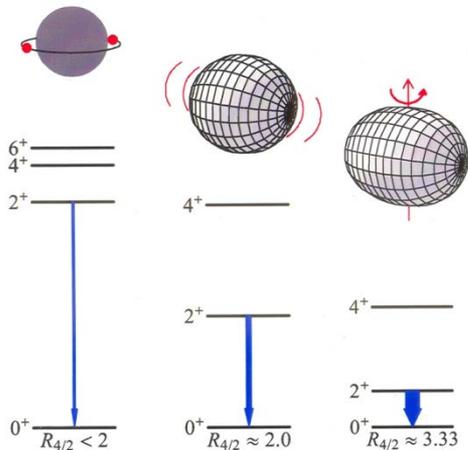
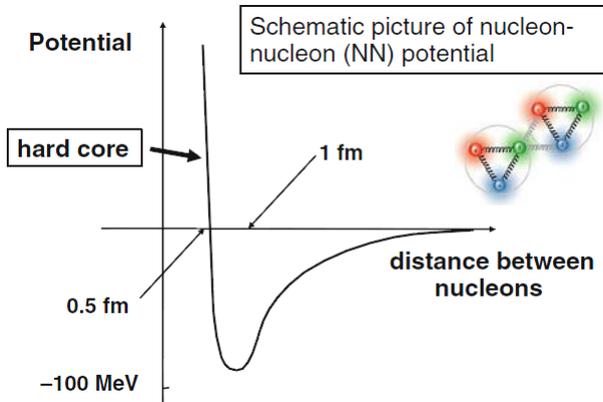


The Why and How of Radioactive-Beam Research

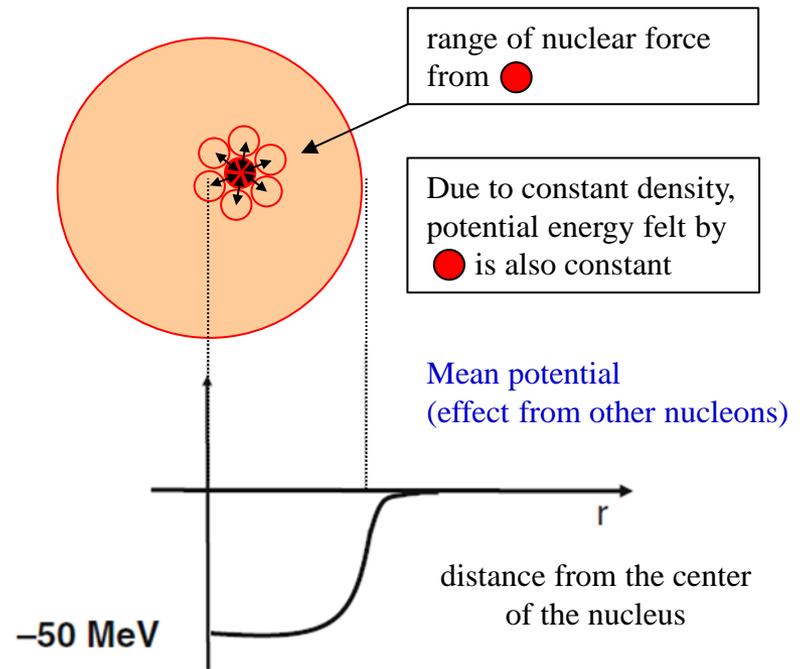


The Why and How of Radioactive-Beam Research

❖ Atomic nuclei are quantum systems with a finite number of strongly interacting fermions: protons and neutrons.



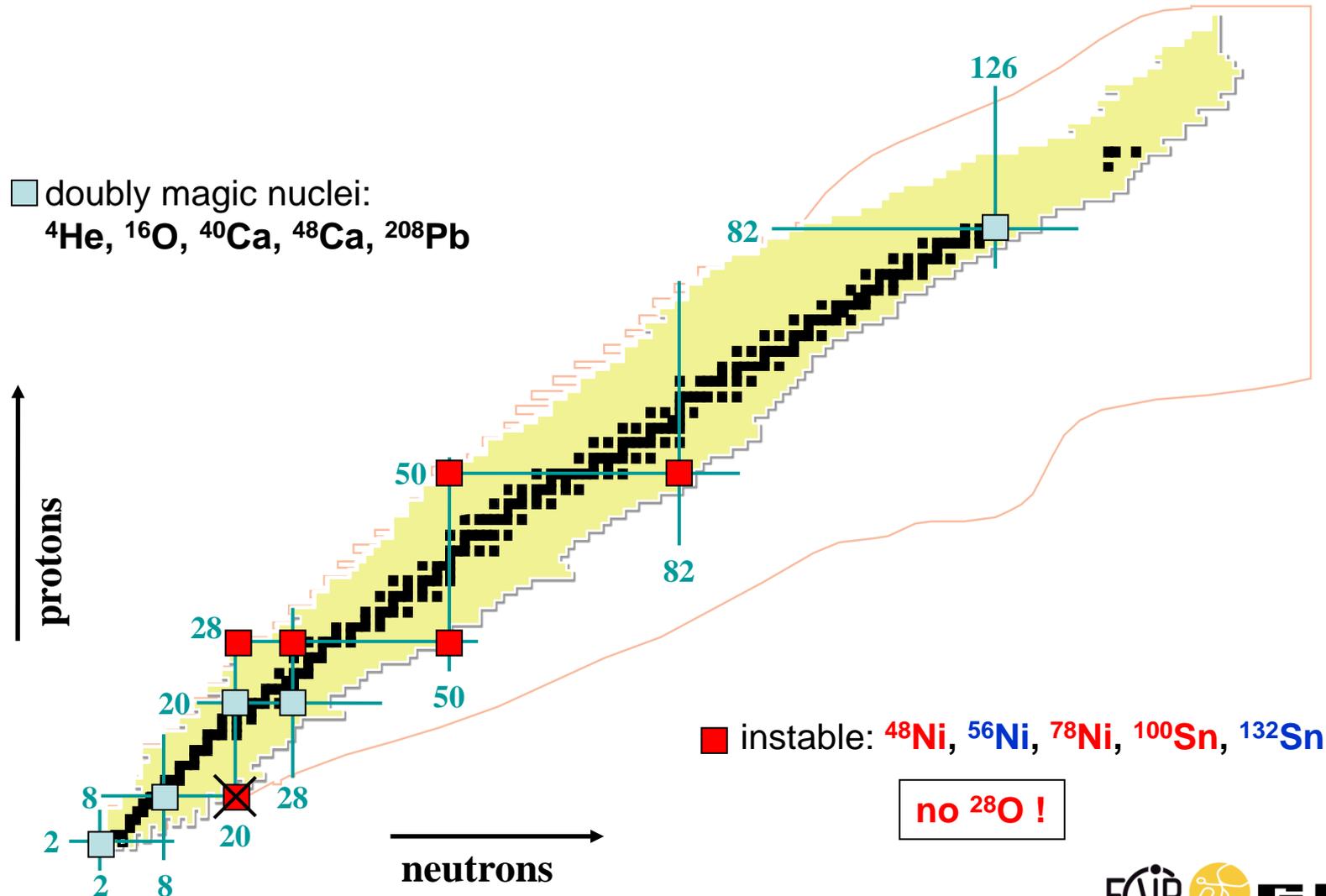
- ❖ Light nuclei up to $A=12$ are described by bare nucleon-nucleon interaction.
- ❖ In heavier nuclei the interactions between the nucleons are modified by the medium → effective interactions are needed.



❖ How can collective phenomena be explained from individual motion?

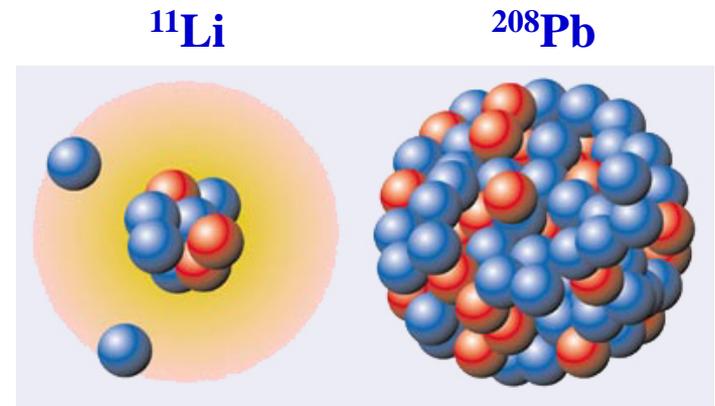
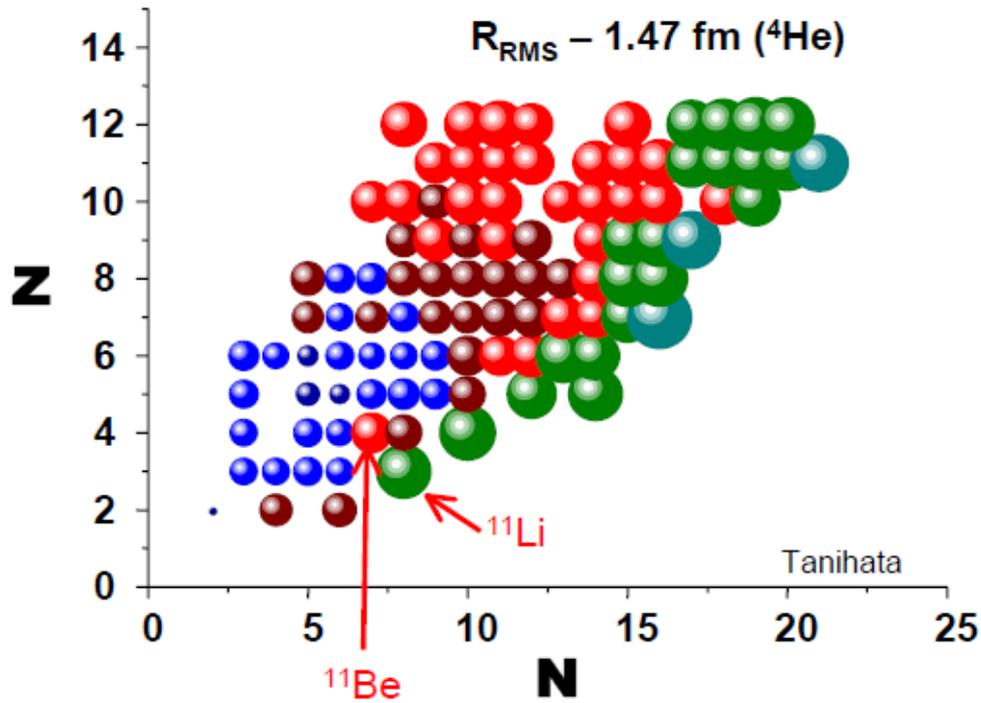
The Nuclear Chart

Our Road Map from Stable to Exotic Nuclei



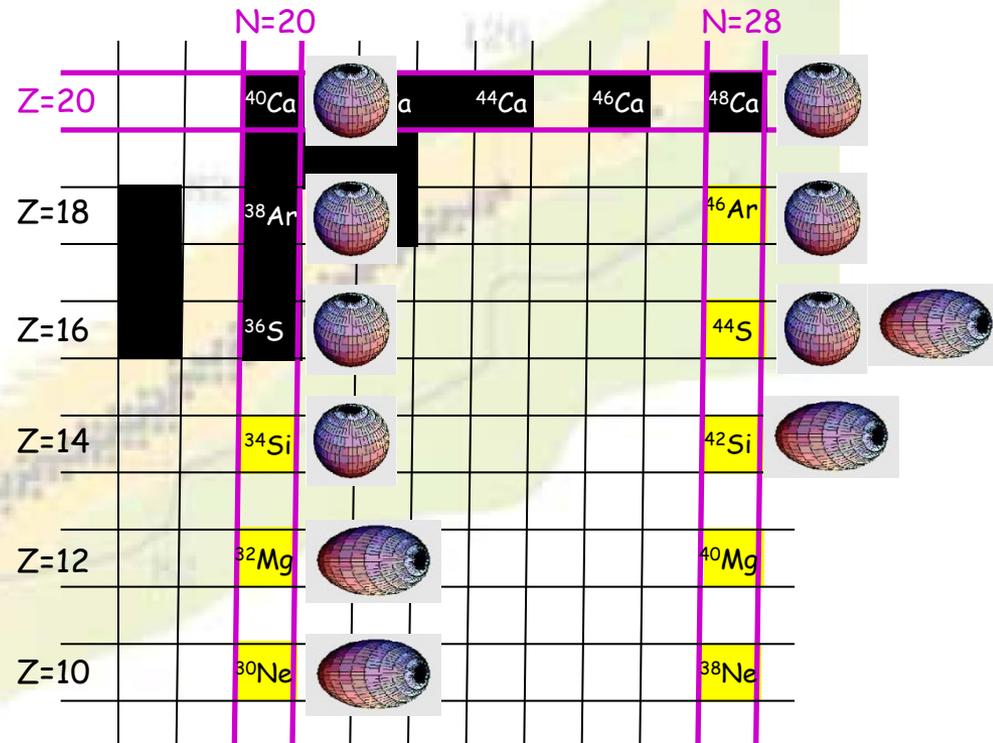
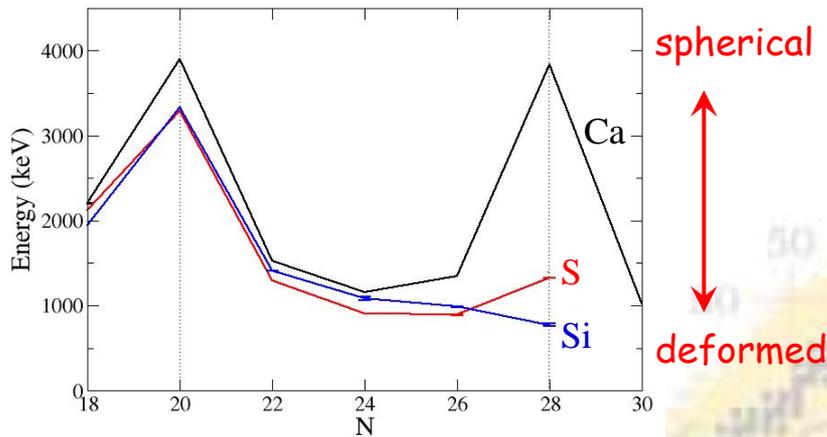
Nuclear radii

❖ textbooks says: $R=1.2 \cdot A^{1/3}$



Nuclear shell structure

Experimental evidence of magic numbers

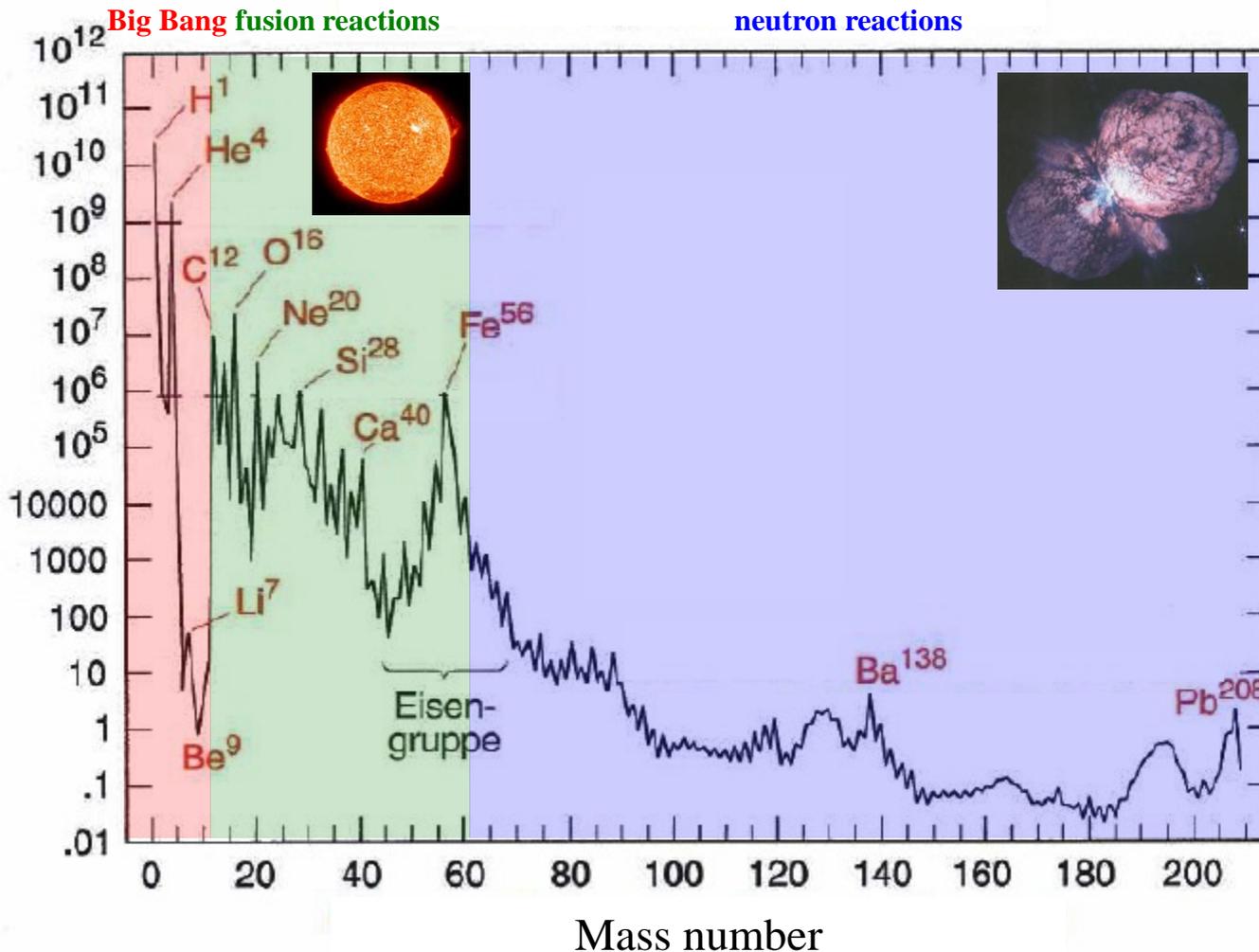


Indicators for nuclear shell model:

high energies of 2_1^+ state
for nuclei with magic numbers

Solar abundances of elements

Solar abundance ($\text{Si}^{28} = 10^6$)



open questions:

- Why is Fe more common than Au ?
- Why do the heavy elements exist and how are they produced?
- Can we explain the solar abundances of the elements?

The chart of nuclides

Nucleosynthesis in the r-process

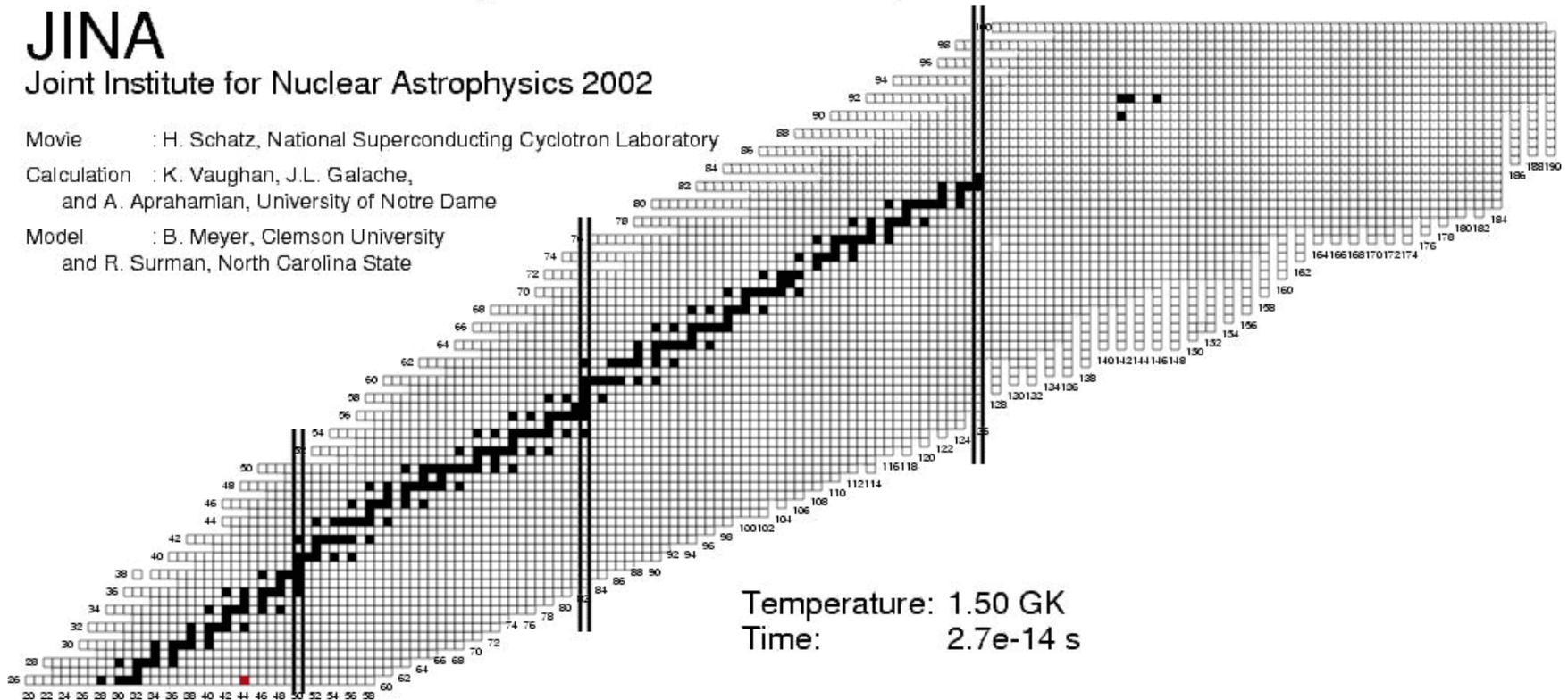
JINA

Joint Institute for Nuclear Astrophysics 2002

Movie : H. Schatz, National Superconducting Cyclotron Laboratory

Calculation : K. Vaughan, J.L. Galache,
and A. Aprahamian, University of Notre Dame

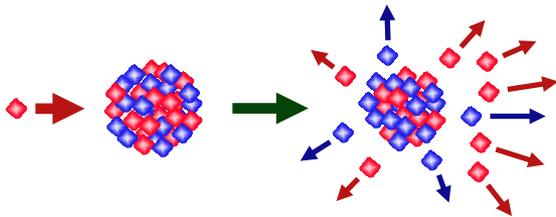
Model : B. Meyer, Clemson University
and R. Surman, North Carolina State



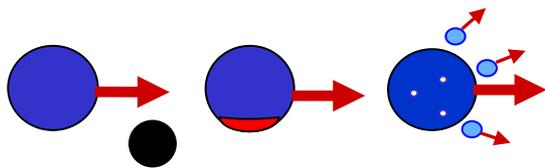
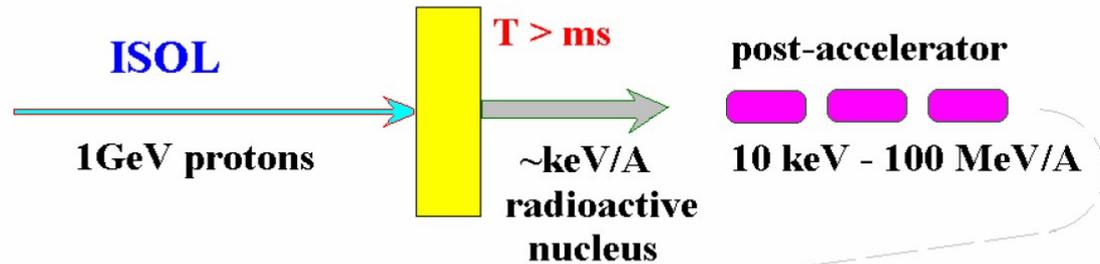
Spallation & Projectile Fragmentation Reactions

A Route to Exotic Nuclei

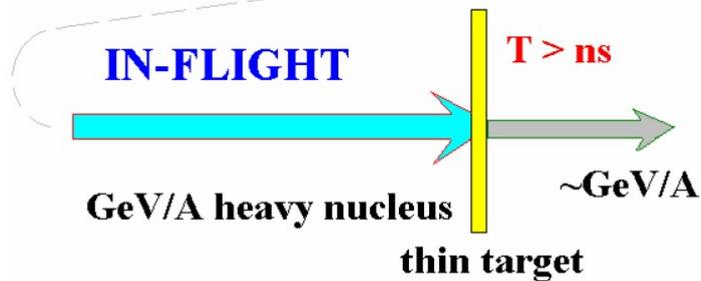
Spallation



thick target +
ion source



Fragmentation



High-energy proton-induced nuclear reactions

Some early high-energy proton accelerators:

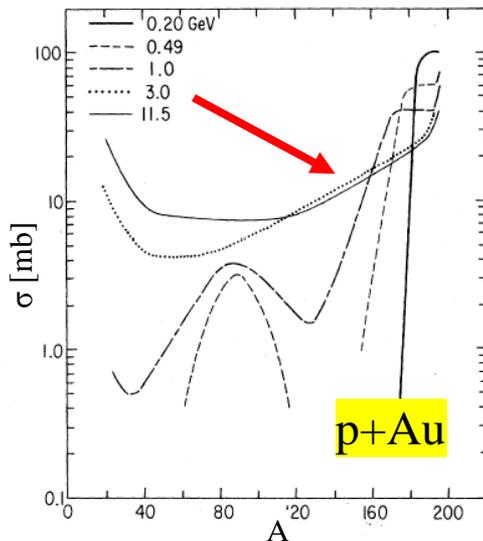
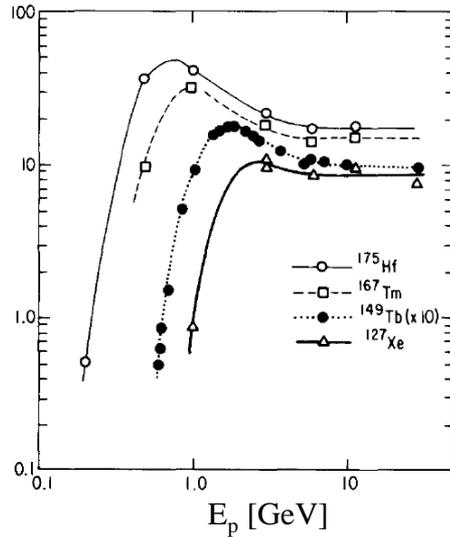
Facility	Energy	from year
Bevatron (Berkeley)	6 GeV	1954.....
AGS (Brookhaven)	11 GeV	1960.....
Fermilab (Chicago)	>300 GeV	1967.....

They were also used to bombard various stable target materials.

These targets were analyzed with radiochemical methods, i.e. γ -spectroscopy with or without chemical separators

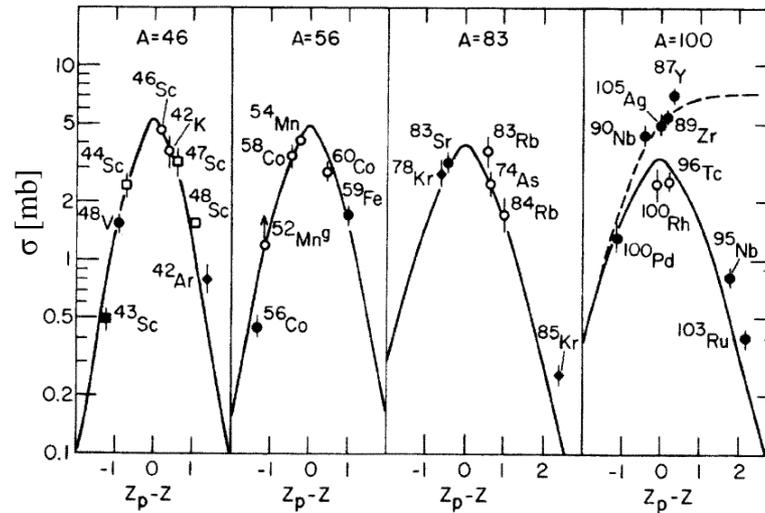
➔ Production cross sections and (some) kinematics for suitable radioactive isotopes

High-energy proton-induced nuclear reactions



Important findings:

- ❖ Energy-independence of cross sections
- ❖ Bell-shaped Z-distribution for constant A



- ❖ Mass yields: exponential slope

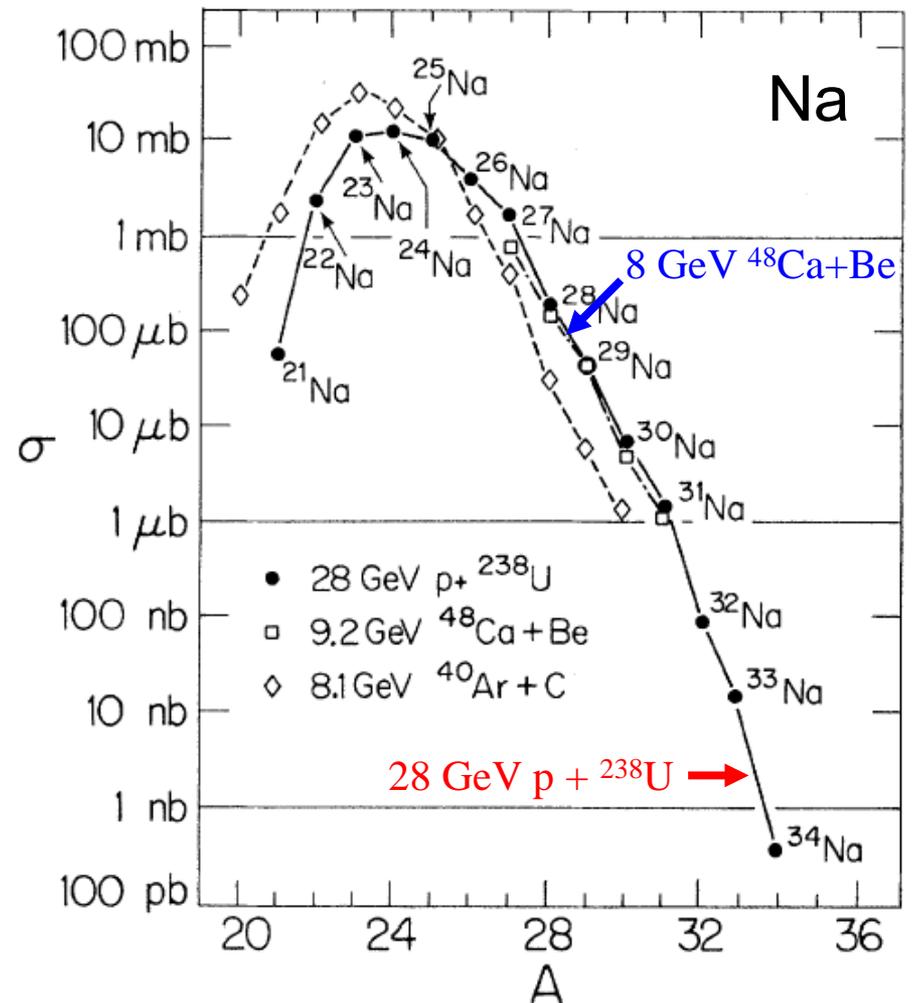
Proton- versus heavy-ion induced reactions

Proton- and heavy-ion induced reactions give very similar isotope distribution:

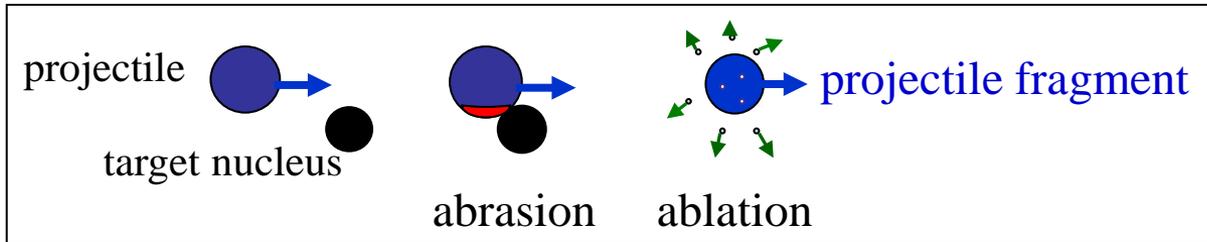
Target fragmentation: $\text{GeV } p + A_{\text{target}} \rightarrow A$

Projectile fragmentation: $\text{GeV/u } A_{\text{proj}} + p \rightarrow A$

are equivalent



Projectile fragmentation reactions



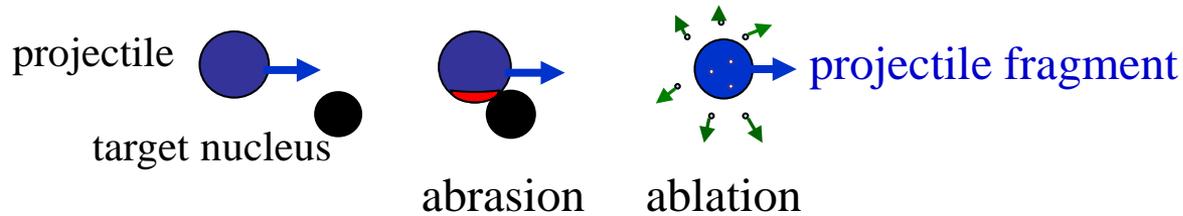
At GeV energies nucleons can be regarded as a classical particles

- Nucleon-nucleon collisions can be treated classically using measured free nucleon-nucleon cross sections (intra-nuclear cascade).
- In these collisions very *little transfer momentum* is exchanged.
- After the cascade the residual nucleus is *highly excited*.
- Heavy-ion projectiles can be treated as a bag of individual nucleons.

Physical models: Two-step approach

- Step 1: **Intranuclear-cascade** models or **Abrasion** models
- Step 2: **Evaporation** calculation

Projectile fragmentation reactions



Empirical parameterization of fragmentation cross section:

EPAX v.3 K. Sümmerer, Phys. Rev. C86 (2012) 014601
<http://web-docs.gsi.de/~weick/epax/>

EPAX V3, Empirical parametrization of fragmentation cross sections
by Klaus Sümmerer, March 2012

projectile:		target:		fragment:	
A_p	Z_p	A_t	Z_t	A_f	Z_f
58	28	9	4	48	28

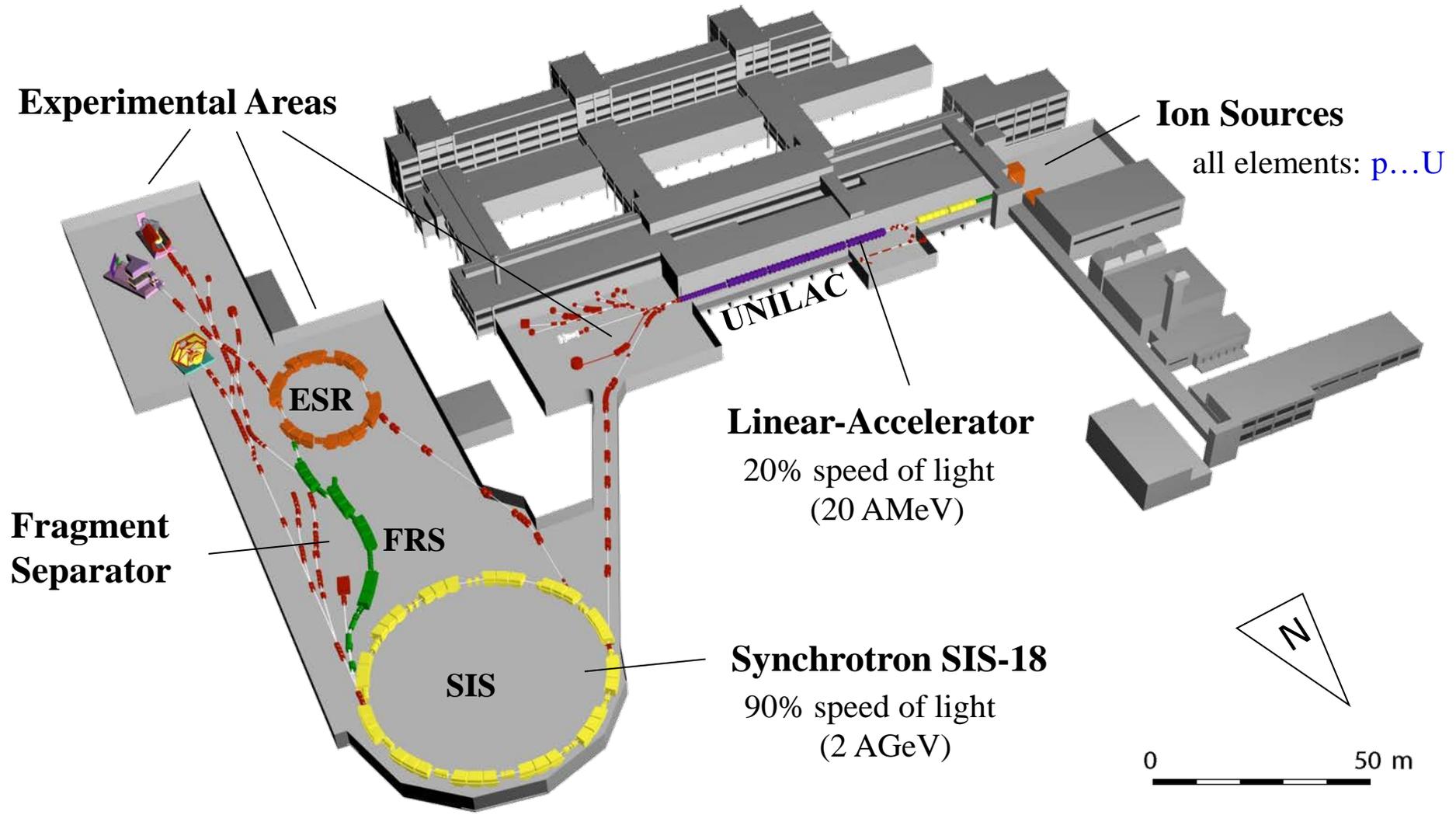
calculate

EPAX V3, Empirical parametrization of fragmentation cross sections

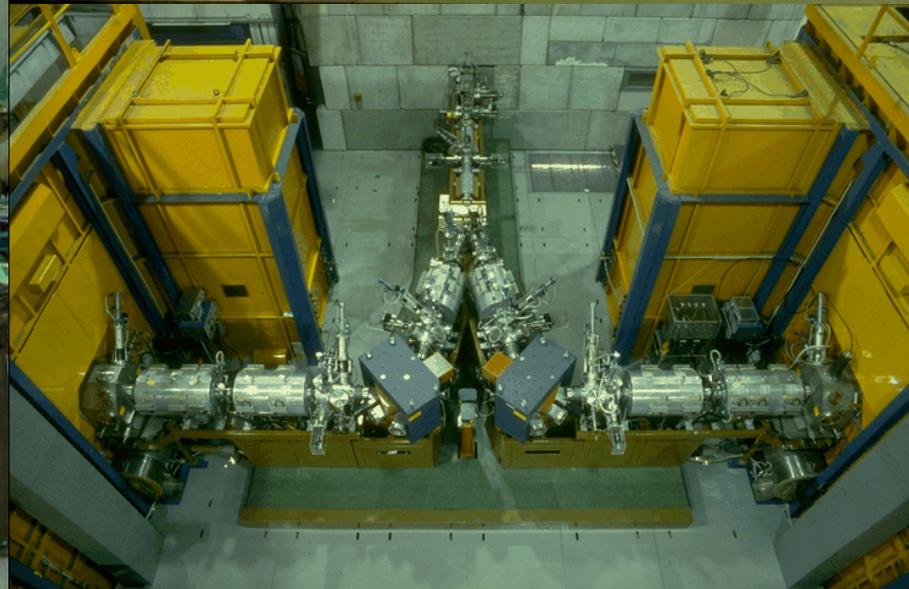
EPAX Version 3.1
by Klaus Sümmerer, 15.03.2012

Fragmentation cross section !!:
projectile $A_p=58.000000$ $Z_p=28.000000$
on target $A_t=9.000000$ $Z_t=4.000000$
to produce $A_f=48.000000$ $Z_f=28.000000$
 $\sigma = 1.407530e-14$ b

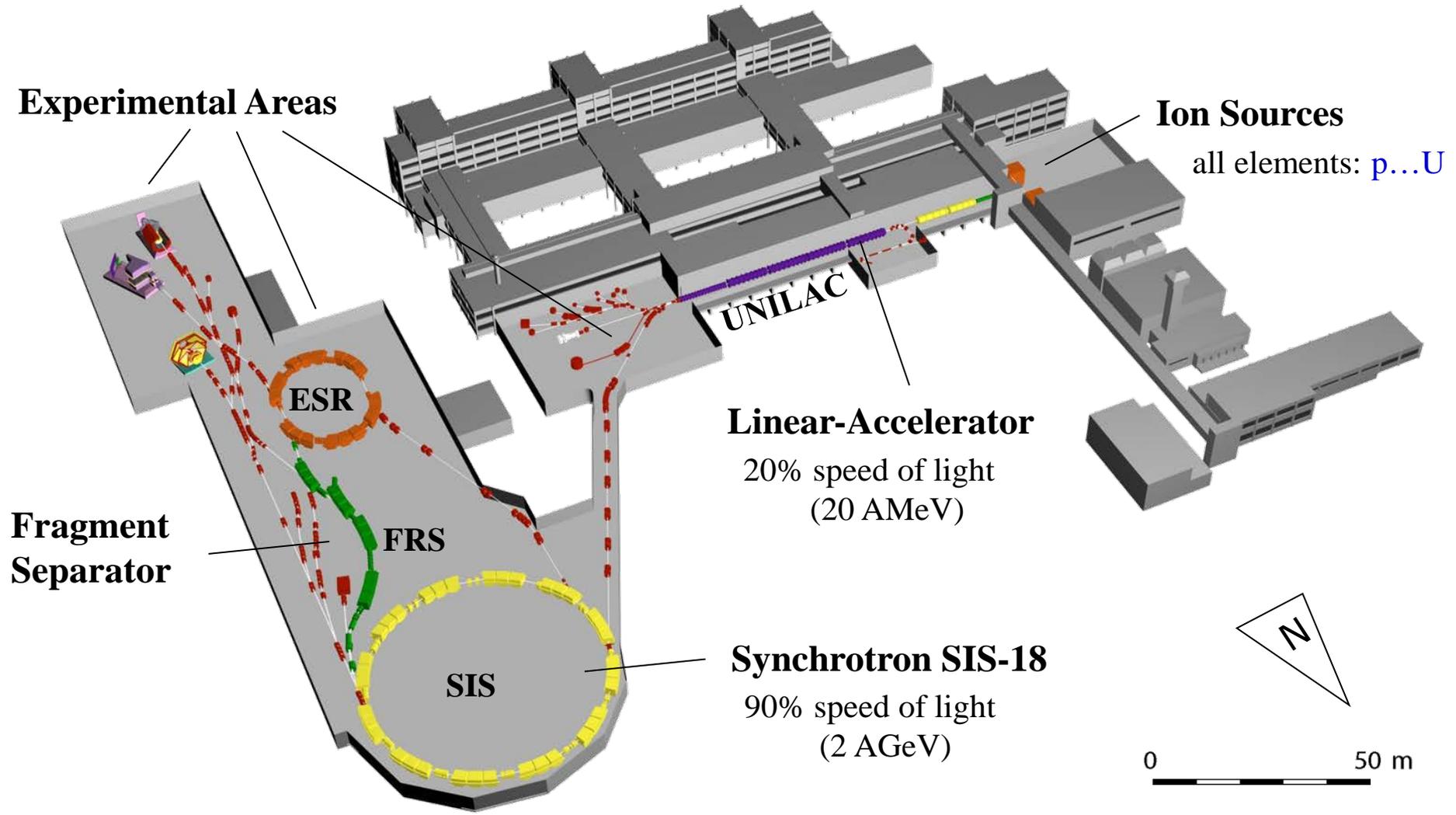
The Accelerator Facility at GSI



UNILAC Accelerator

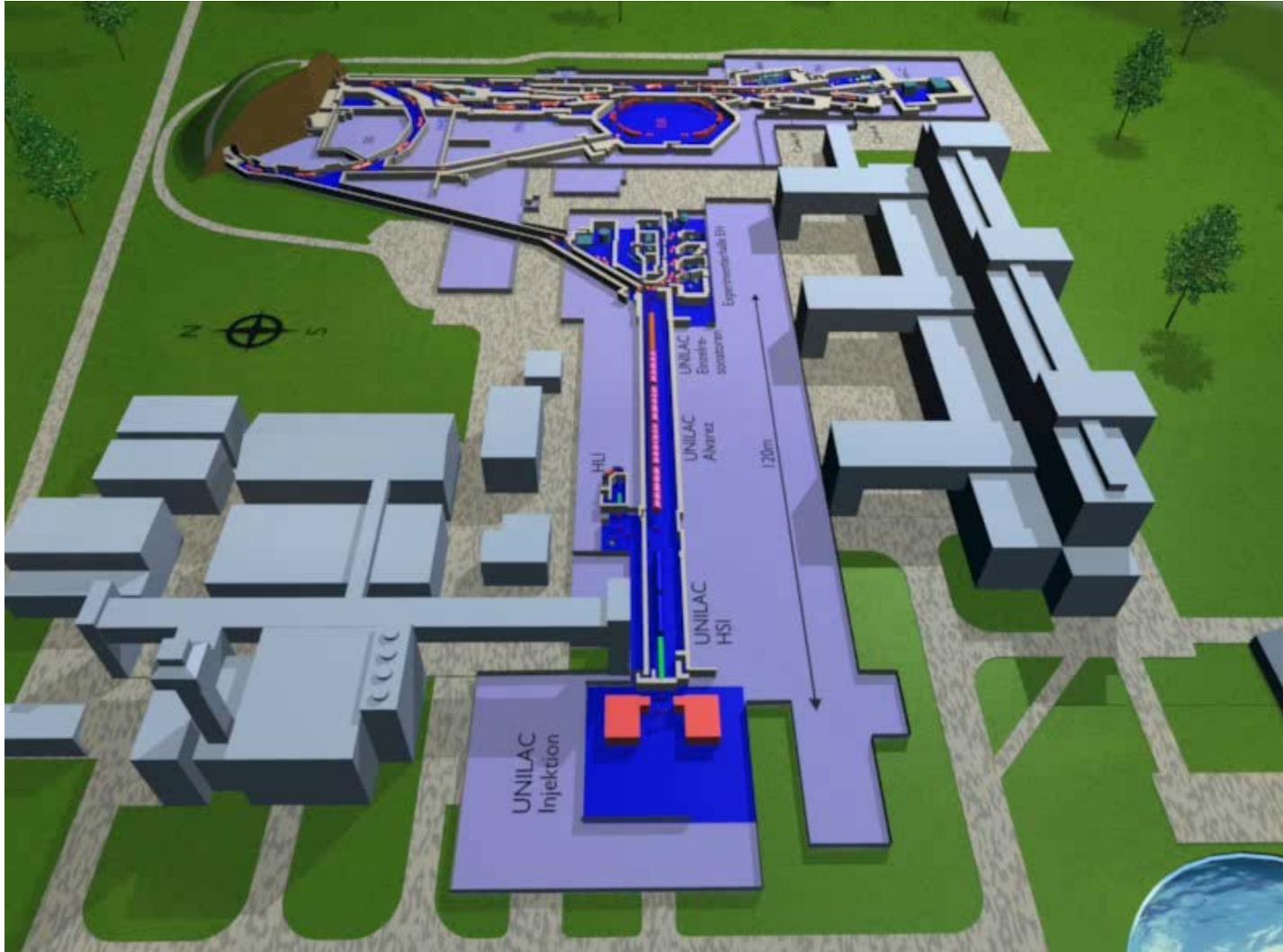


The Accelerator Facility at GSI

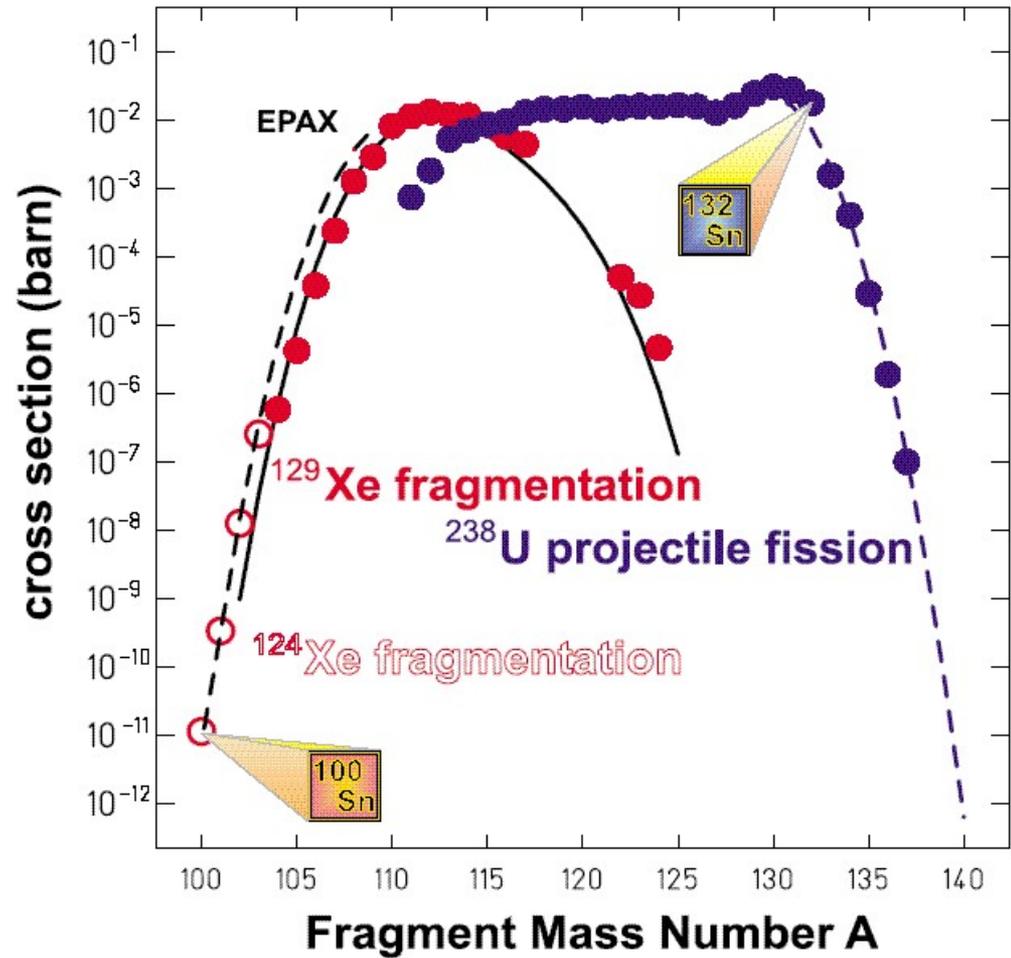
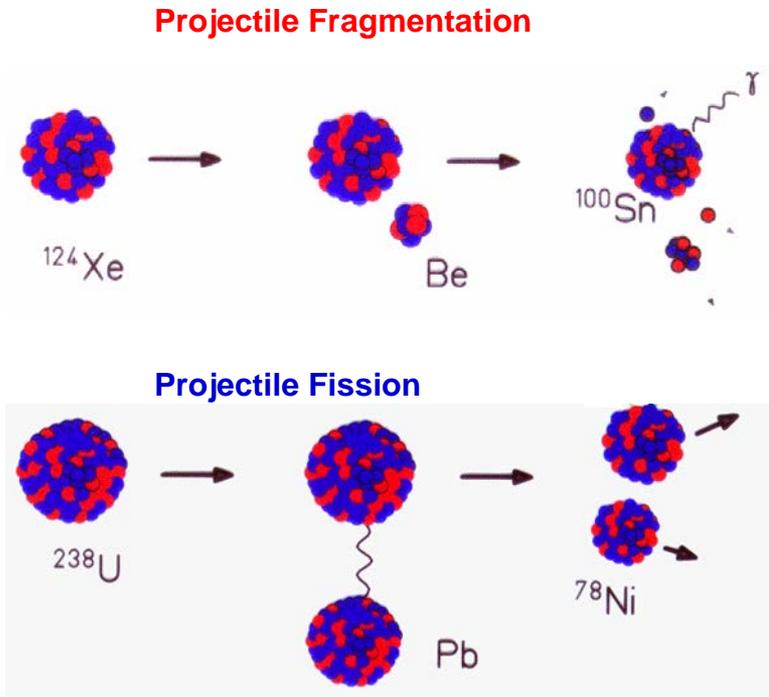




Where do we do the experiments?



Projectile fragmentation reactions

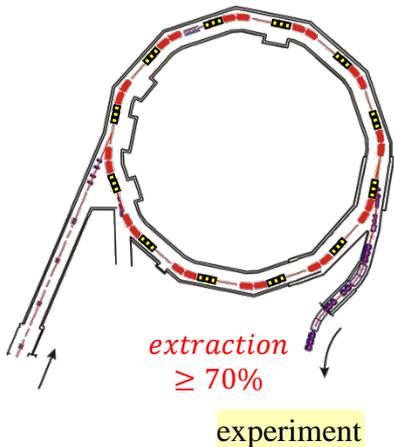
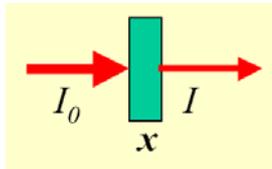
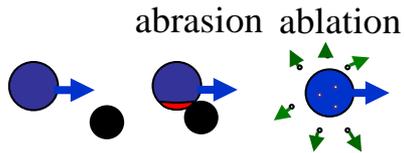


Nuclear Reaction Rate

➤ nuclear reaction rate [s^{-1}] = luminosity [$\text{atoms cm}^{-2} s^{-1}$] * σ_f [cm^2]

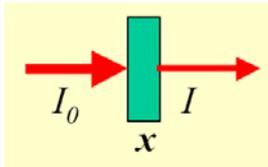
➤ σ_f [cm^2] for projectile fragmentation + fission

➤ luminosity [$\text{atoms cm}^{-2} s^{-1}$] = projectiles [s^{-1}] * target nuclei [cm^{-2}]



Ion	SIS-18 (2008)	SIS-100 (expected)	
$^{20}\text{Ne}^{10+}$	$2 \cdot 10^{11}$	$^{20}\text{Ne}^{7+}$	$1.6 \cdot 10^{12}$
$^{40}\text{Ar}^{18+}$	$1 \cdot 10^{11}$	$^{40}\text{Ar}^{10+}$	$1.4 \cdot 10^{12}$
$^{58}\text{Ni}^{26+}$	$9 \cdot 10^{10}$	$^{58}\text{Ni}^{14+}$	$1.3 \cdot 10^{12}$
$^{84}\text{Kr}^{34+}$	$8 \cdot 10^{10}$	$^{84}\text{Kr}^{17+}$	$1.2 \cdot 10^{12}$
$^{132}\text{Xe}^{48+}$	$7 \cdot 10^{10}$	$^{132}\text{Xe}^{22+}$	$1.3 \cdot 10^{12}$
$^{197}\text{Au}^{65+}$	$5 \cdot 10^{10}$	$^{197}\text{Au}^{25+}$	$1.2 \cdot 10^{12}$
$^{238}\text{U}^{73+}$	$1.6 \cdot 10^{10}$	$^{238}\text{U}^{92+}$	$1.4 \cdot 10^{10}$
$^{238}\text{U}^{28+}$	$1.4 \cdot 10^{10}$	$^{238}\text{U}^{28+}$	$5.0 \cdot 10^{11}$

Nuclear Reaction Rate



density ρ

Primary reaction rate:

$$\phi_f [s^{-1}] \cong \phi_p [s^{-1}] \cdot \frac{x [g/cm^2] \cdot 6.02 \cdot 10^{23}}{A_t [g]} \cdot \sigma_f [cm^2]$$

(thin target)

Example: ^{238}U (10^9s^{-1}) on ^{208}Pb ($x=1\text{g/cm}^2$) \rightarrow ^{132}Sn ($\sigma_f=15.4\text{mb}$) reaction rate: $44571 [s^{-1}]$

Example: ^{124}Xe (10^9s^{-1}) on ^9Be ($x=1\text{g/cm}^2$) \rightarrow ^{104}Sn ($\sigma_f=5.6\mu\text{b}$) reaction rate: $375 [s^{-1}]$

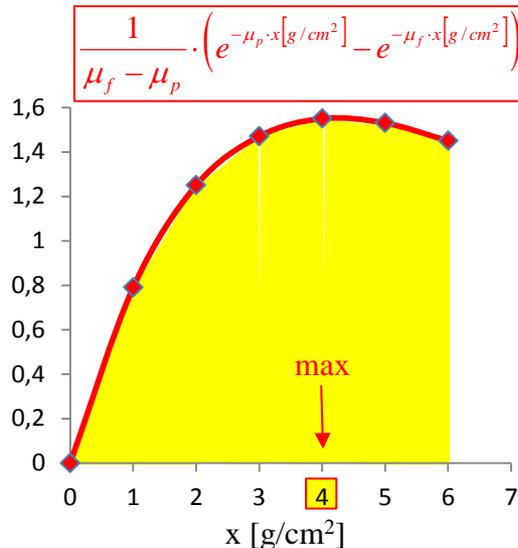
The **optimum thickness** of the production target is limited by the loss of fragments due to secondary reactions

Primary + secondary reaction rate:

$$\phi_f [s^{-1}] = \phi_p [s^{-1}] \cdot \frac{6.02 \cdot 10^{23} \cdot \sigma_f [cm^2]}{A_t [g]} \cdot \frac{1}{\mu_f - \mu_p} \cdot (e^{-\mu_p \cdot x [g/cm^2]} - e^{-\mu_f \cdot x [g/cm^2]})$$

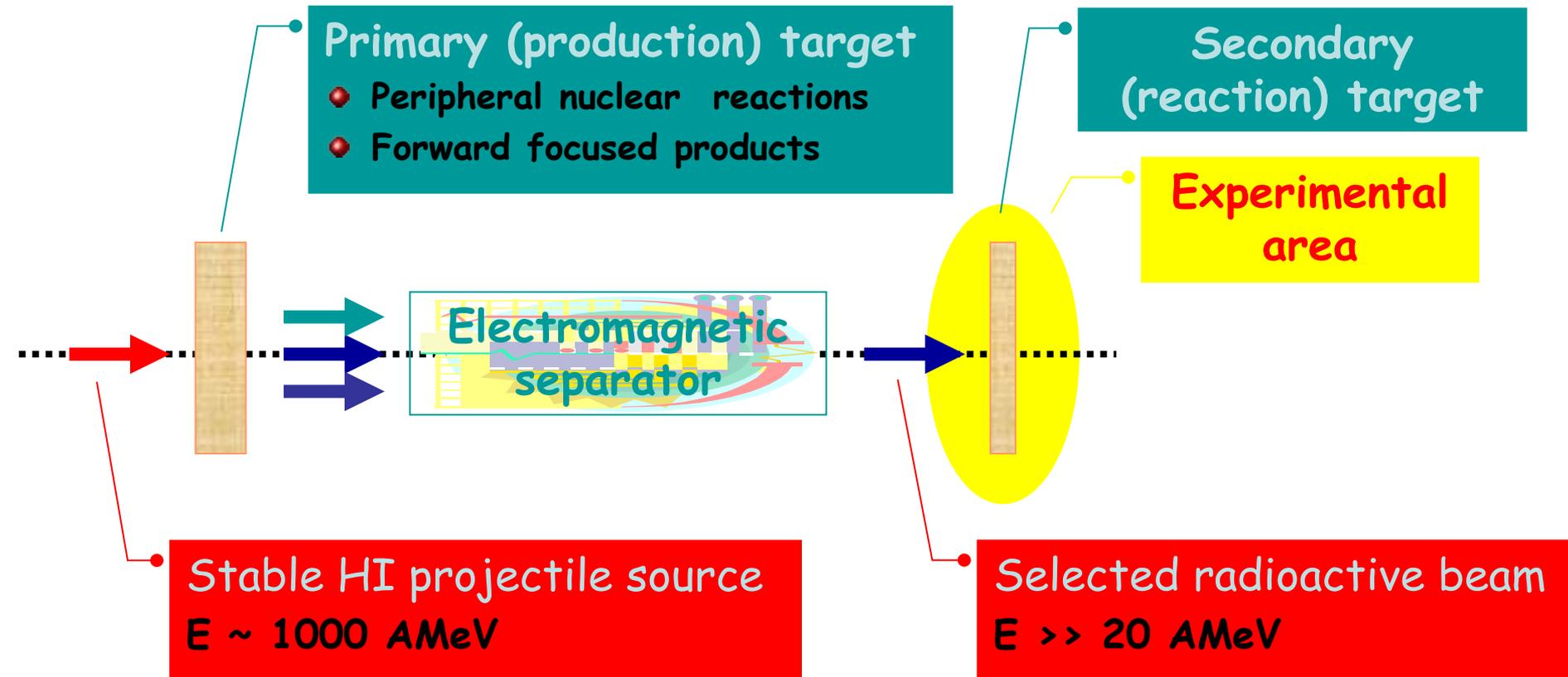
$$\text{with } \mu = \frac{6.02 \cdot 10^{23}}{A_2 [g]} \cdot \sigma_{\text{reaction}} [cm^2]$$

Example: ^{124}Xe on $^9\text{Be} \rightarrow ^{104}\text{Sn}$, $\sigma(^{124}\text{Xe}+^9\text{Be}) = 3.65[b] \rightarrow \mu_p = 0.244 [cm^2/g]$
 $\sigma(^{104}\text{Sn}+^9\text{Be}) = 3.44[b] \rightarrow \mu_f = 0.230 [cm^2/g]$

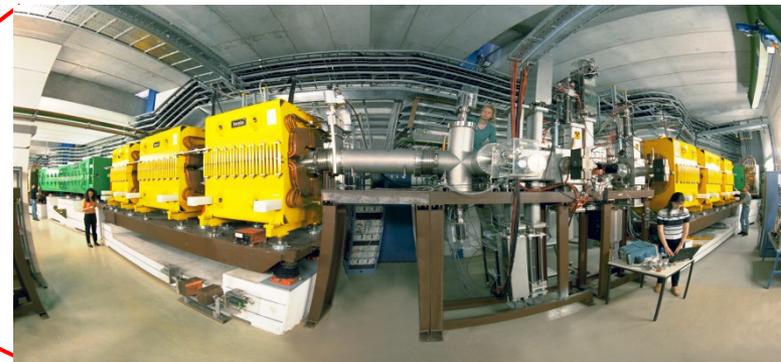
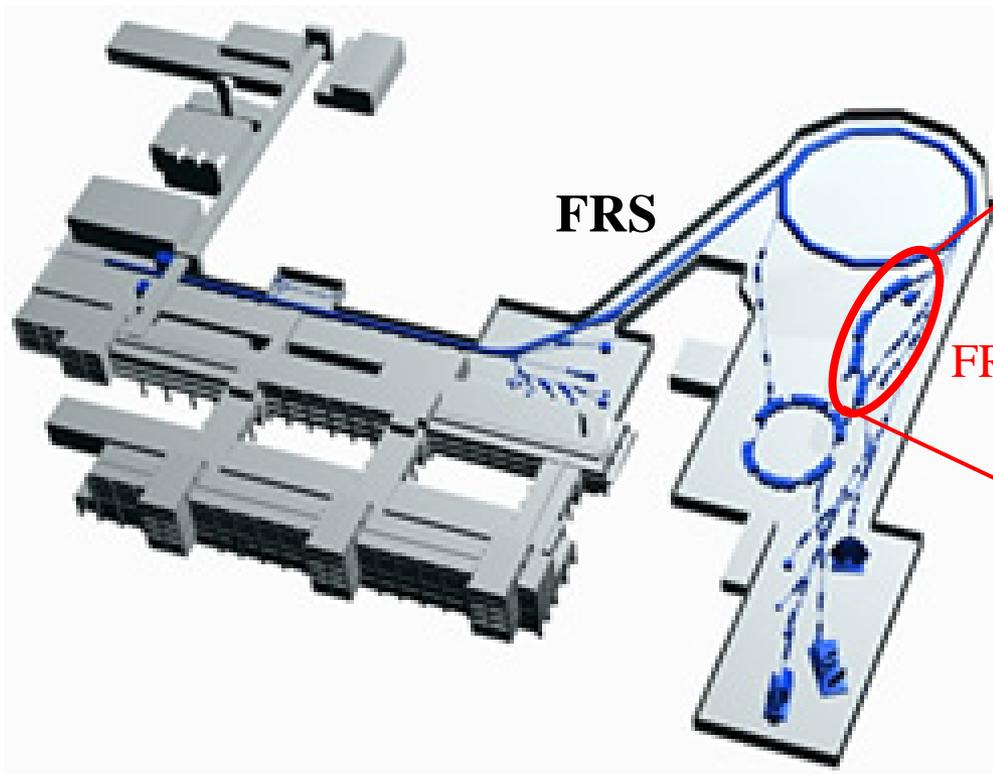
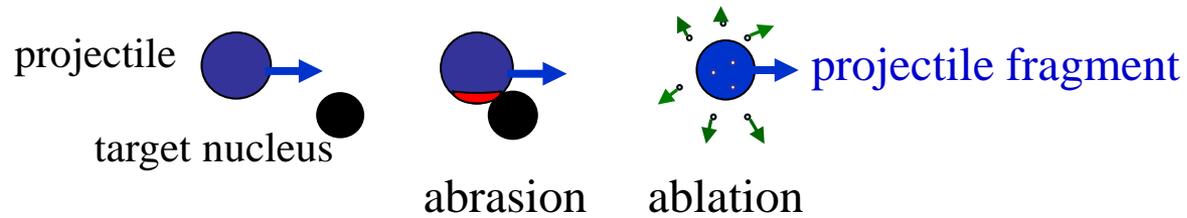


$$\phi_f [s^{-1}] = \phi_p [s^{-1}] - \phi [s^{-1}] = \phi_p [s^{-1}] \cdot \{1 - e^{-N_t [cm^{-2}] \cdot \sigma_f [cm^2]}\} \text{ (thick target)}$$

In-Flight Separation of **R**adioactive **I**on **B**eams

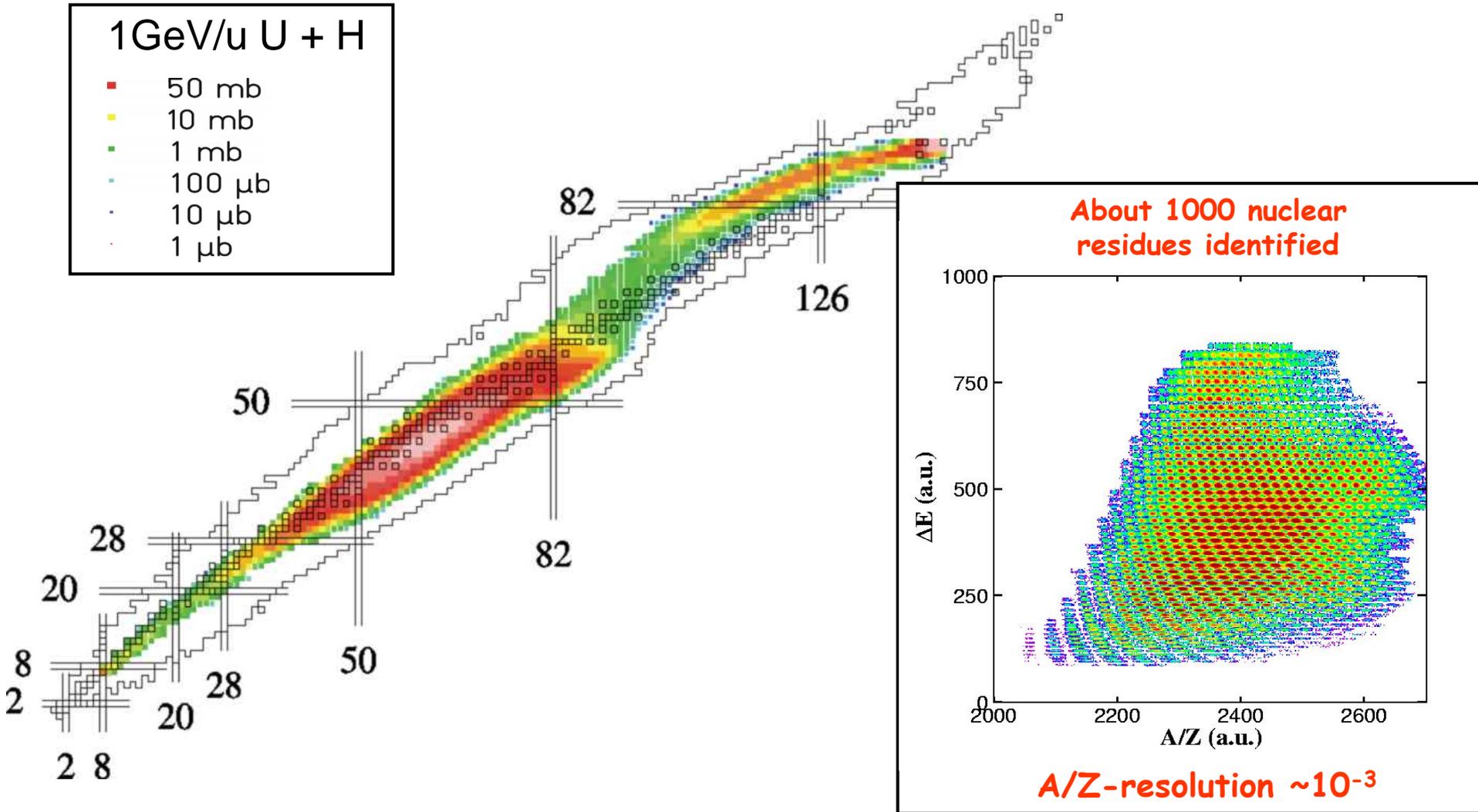


Fragmentation at Relativistic Energies

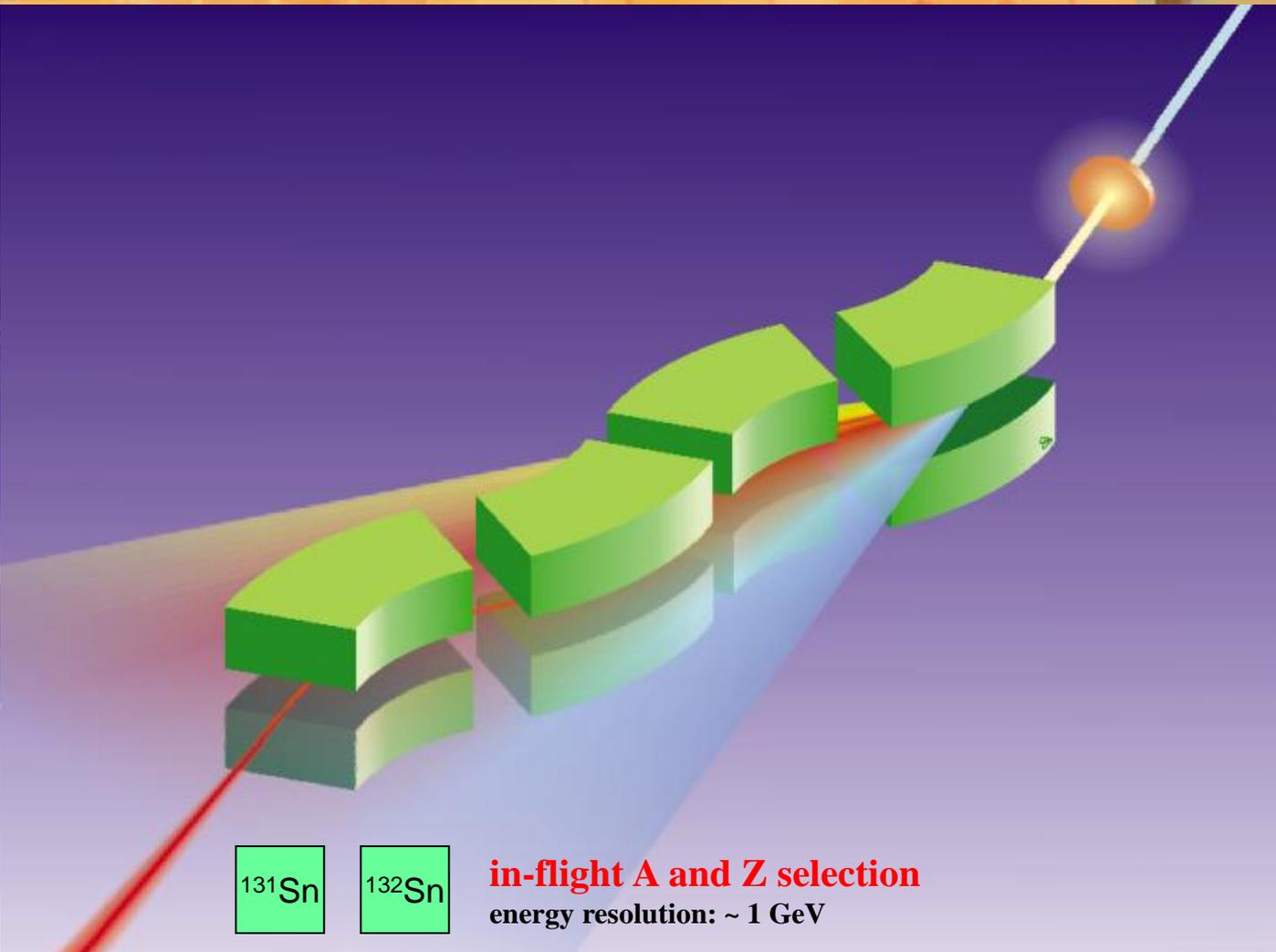


FRagment **S**eparator

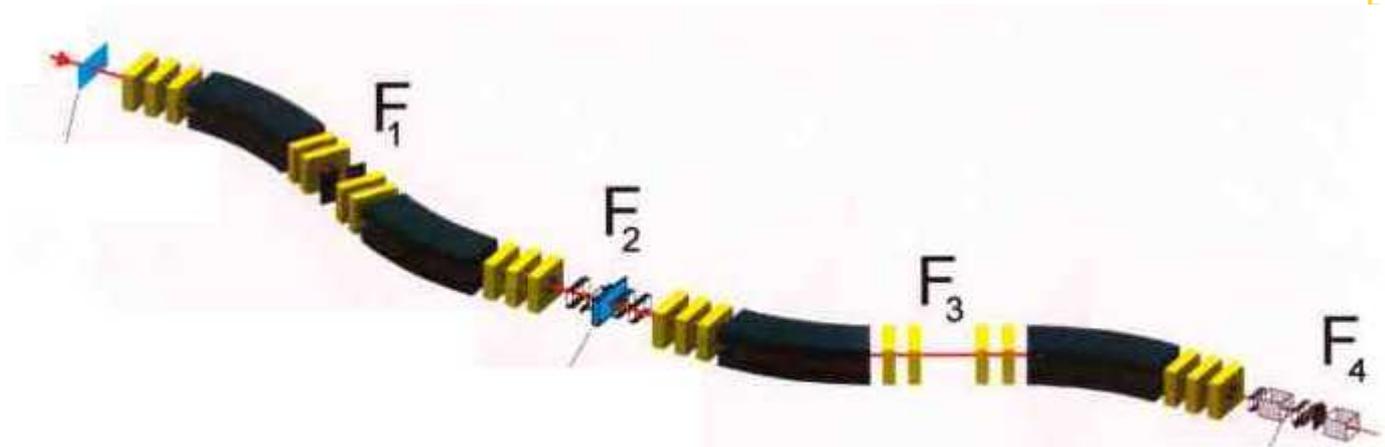
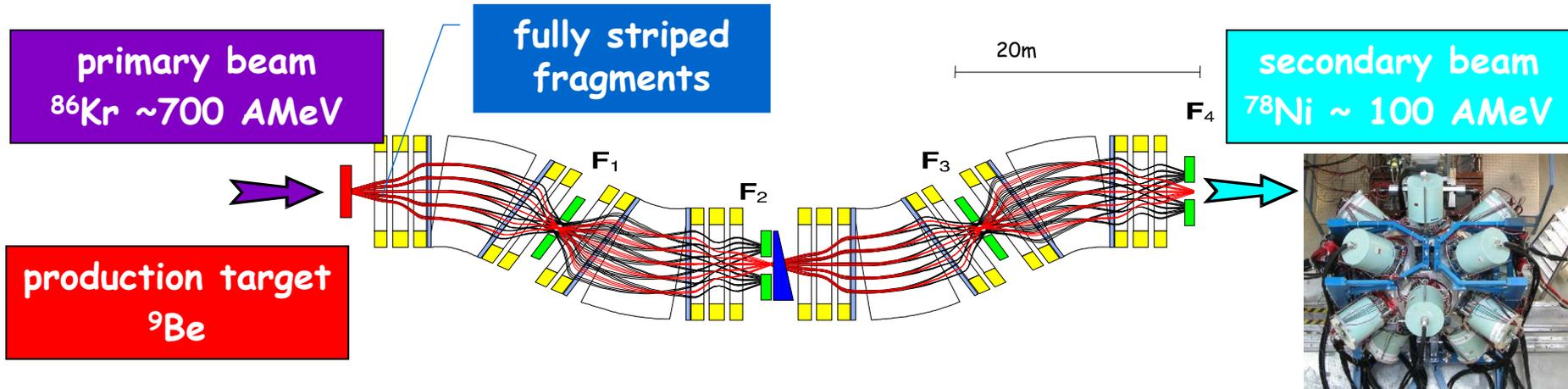
Radioactive Ion Beams at GSI



FRagment Separator at GSI

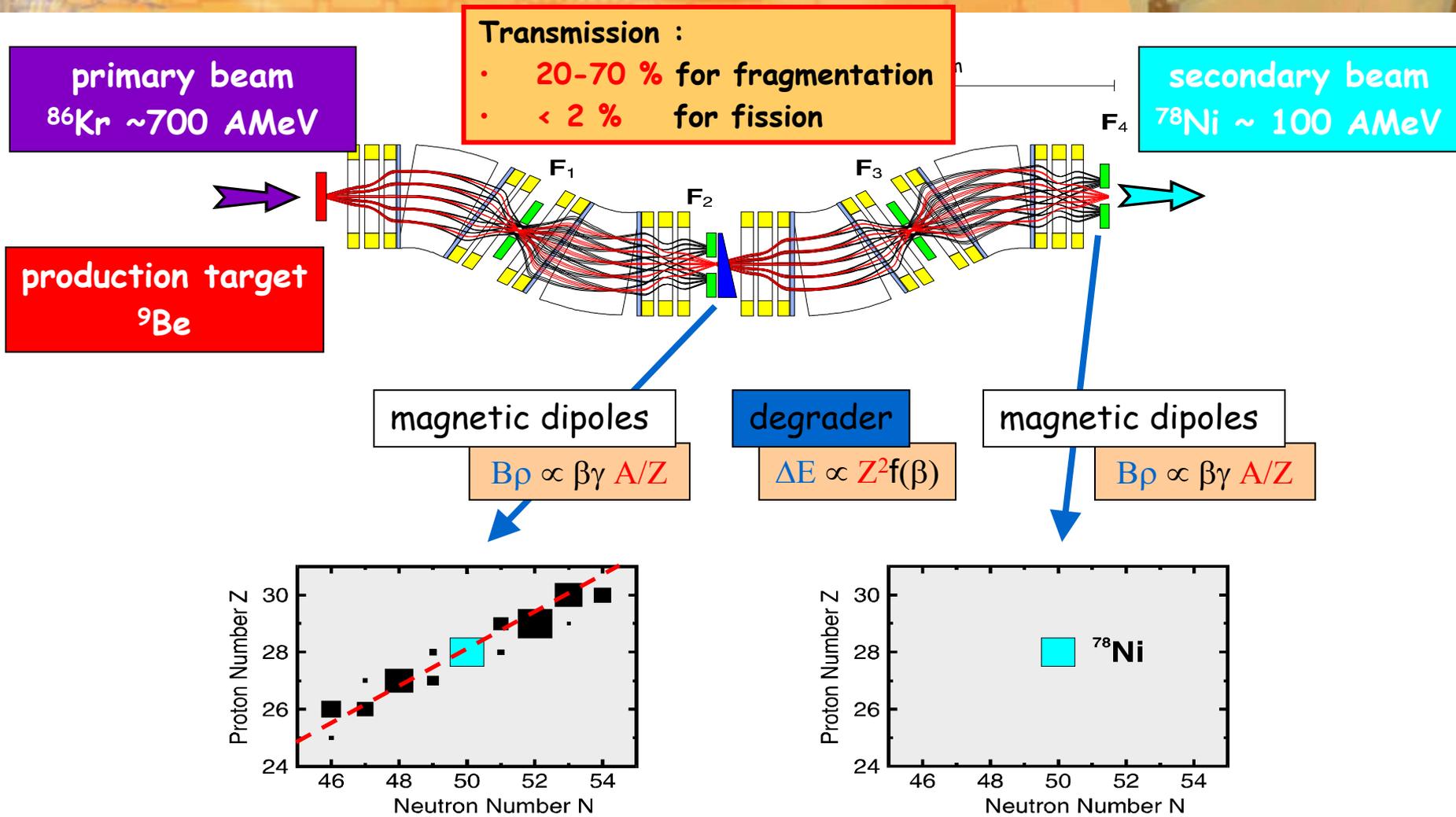


Rare Isotope Selection at FRS: $B\rho$ - ΔE - $B\rho$ Selection

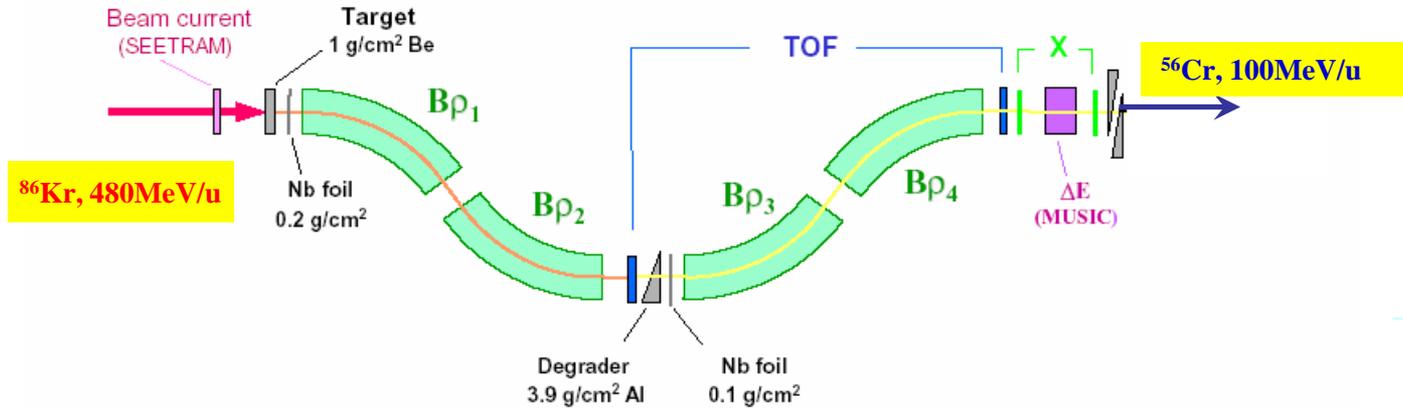
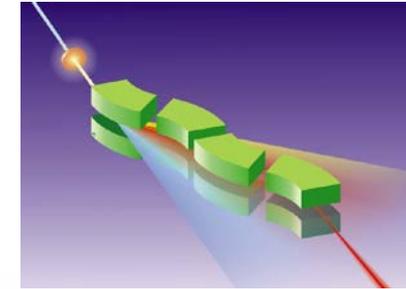
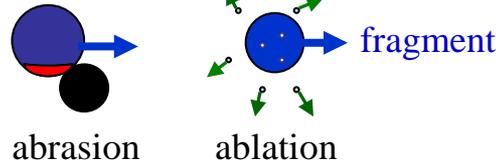


ISING

Rare Isotope Selection at FRS: $B\rho$ - ΔE - $B\rho$ Selection



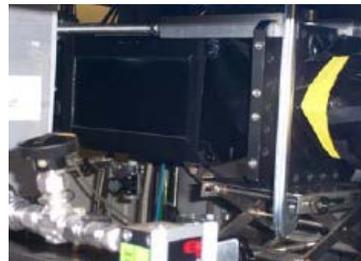
Production, Separation, Identification



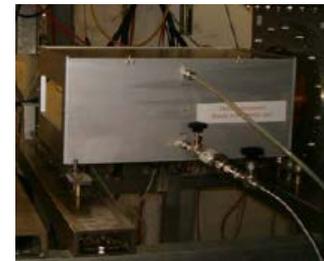
Standard FRS detectors



TPC-x,y
position
@ S2,S4

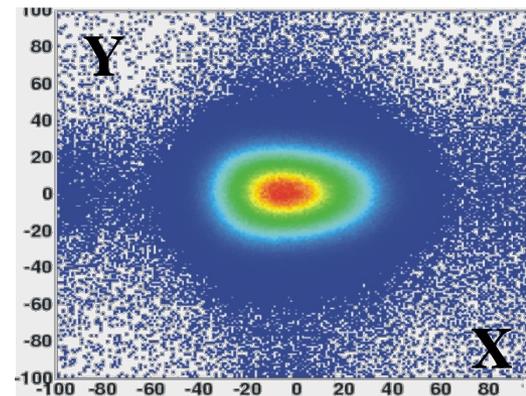
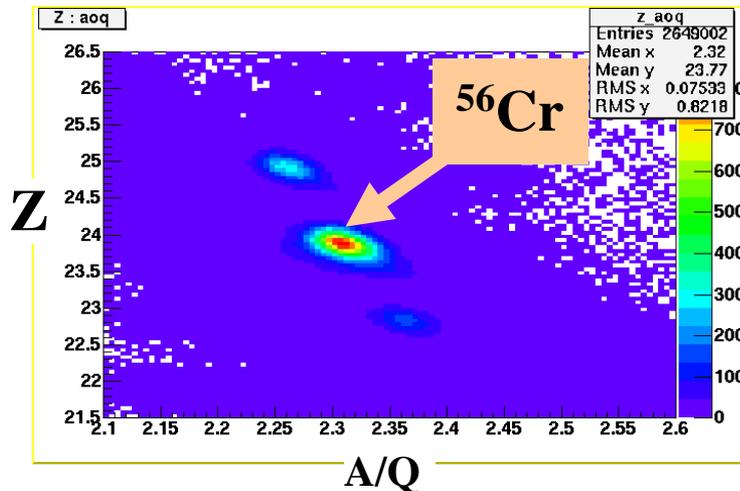
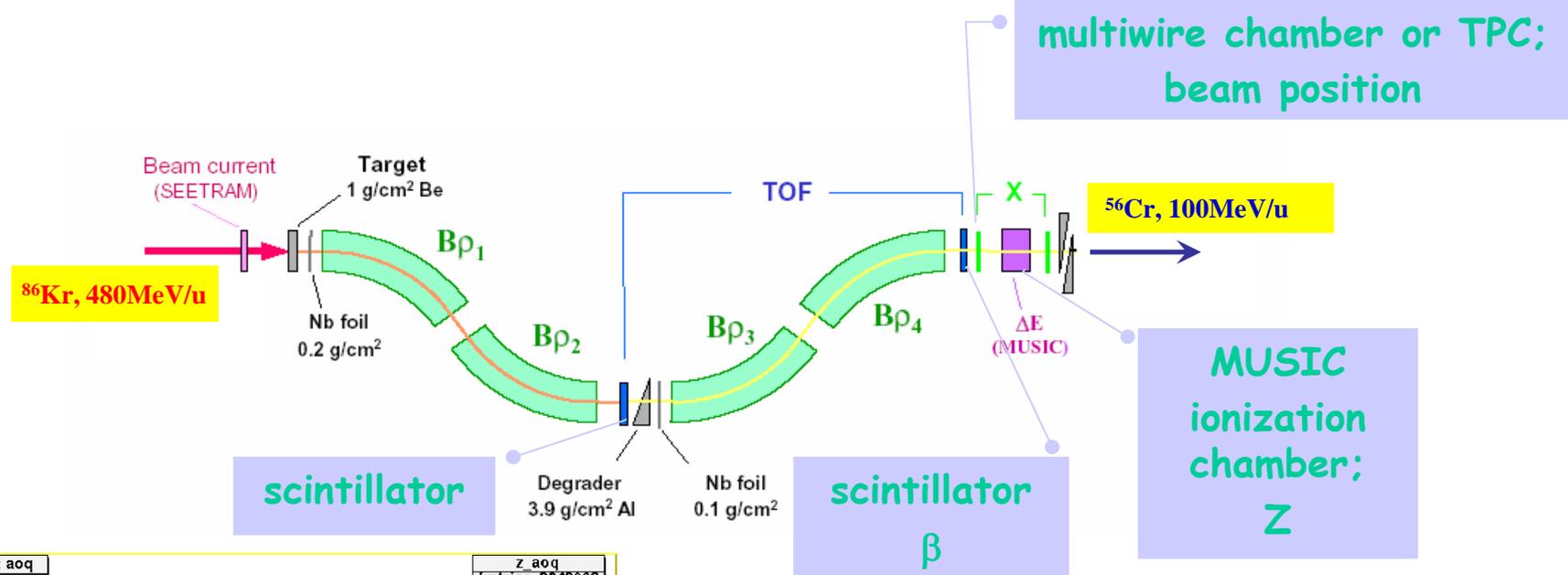


Plastic
scintillator
(TOF)
@ S4

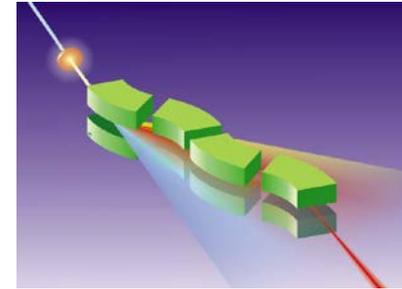
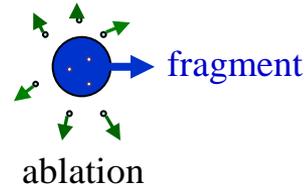
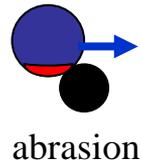


MUSIC
(ΔE)
@ S4

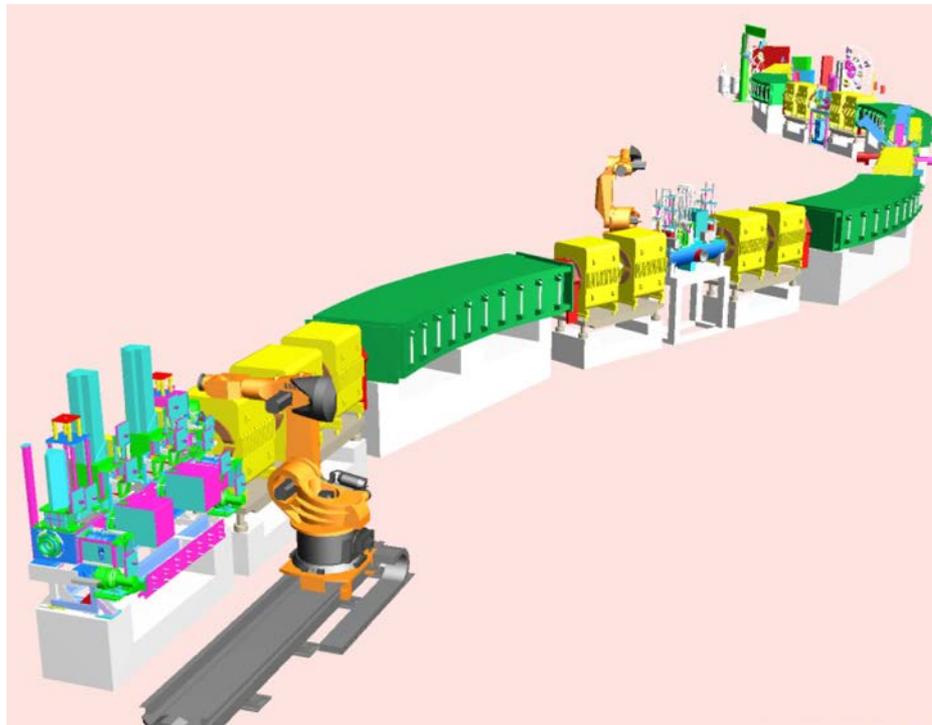
Production, Separation, Identification



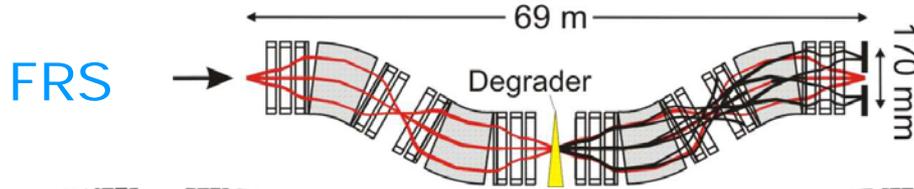
Production, Separation, Identification



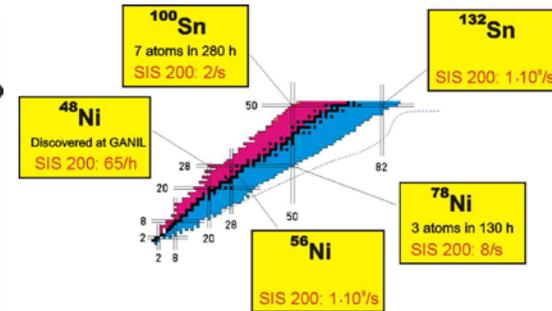
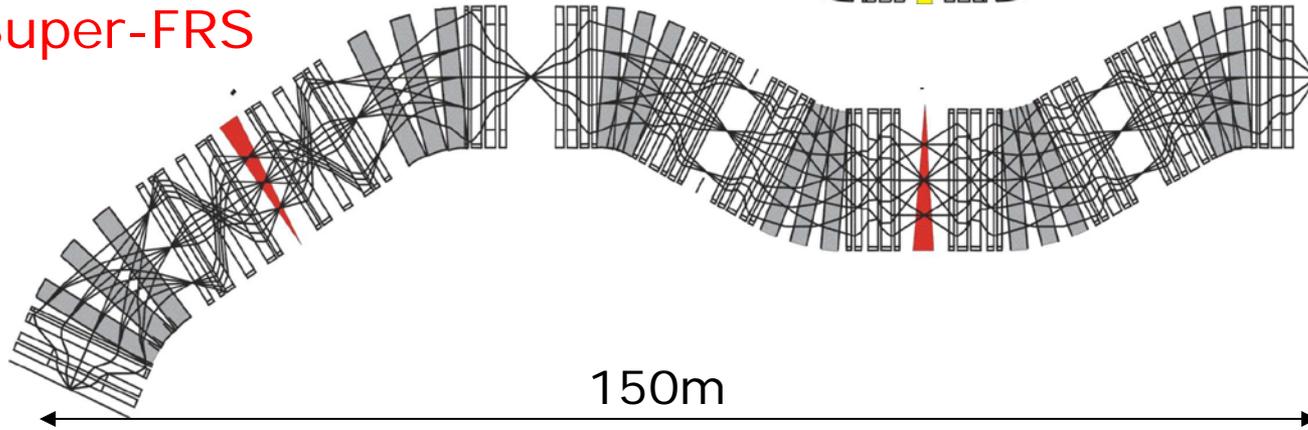
FRagment
Separator



Comparison of FRS with Super-FRS



Super-FRS



	$B\rho_{\max}$	$\Delta p/p$	$\Delta\Phi_x, \Delta\Phi_y$	resolving power	gain factor	
					¹⁹ C	¹³² Sn
FRS	18 Tm	1.0 %	$\pm 13, \pm 13$ mrad	1500	1	1
Super-FRS	20 Tm	2.5 %	$\pm 40, \pm 20$ mrad	1500	5	10
			including primary rate		250	20 000

